

Name : \_\_\_\_\_

Score : \_\_\_\_\_

Teacher : \_\_\_\_\_

Date : \_\_\_\_\_

## Powers of Products and Quotients

Simplify the exponents.

1)  $(2b \cdot 4b^2)^3$

7)  $\left(\frac{5^6}{5}\right)^2$

2)  $(3k^3 \cdot 2k)^2$

8)  $\left(\frac{7^2}{7^5}\right)^3$

3)  $(2b^2 \cdot 3b \cdot b^2)^3$

9)  $\left(\frac{7d^3}{9d}\right)^3$

4)  $(4r^2 \cdot r)^3$

10)  $\left(\frac{k}{k^3}\right)^3$

5)  $(3r^2 \cdot r^3)^2$

11)  $\left(\frac{n^3}{n^5}\right)^3$

6)  $(2w^3 \cdot 3w^2)^3$

12)  $\left(\frac{9r}{3r^5}\right)^3$



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## Operations with Exponents

Simplify the exponents.

1)  $3w^4 \cdot 7w^2h^6$

7)  $\frac{b^3}{b^5}$

2)  $(2y \cdot 4y^3)^3$

8)  $\left(\frac{5y^2s^5}{2y^6s^4}\right)^3$

3)  $\left(\frac{3d^6}{6d}\right)^2$

9)  $(8c^2)^2$

4)  $\frac{w}{w^5}$

10)  $(2z^2 \cdot z^3 \cdot 4z)^3$

5)  $\frac{9y^{-3}}{5y^2}$

11)  $8z^4c^5 \cdot 5zc^6$

6)  $7n \cdot 4n^{-3}$

12)  $\left(\frac{6^4}{6^5}\right)^2$



## Radicals and Rational Exponents

Write each expression in radical form.

1)  $7^{\frac{1}{2}}$

2)  $4^{\frac{4}{3}}$

3)  $2^{\frac{5}{3}}$

4)  $7^{\frac{4}{3}}$

5)  $6^{\frac{3}{2}}$

6)  $2^{\frac{1}{6}}$

Write each expression in exponential form.

7)  $(\sqrt{10})^3$

8)  $\sqrt[6]{2}$

9)  $(\sqrt[4]{2})^5$

10)  $(\sqrt[4]{5})^5$

11)  $\sqrt[3]{2}$

12)  $\sqrt[6]{10}$

Write each expression in radical form.

13)  $(5x)^{-\frac{5}{4}}$

14)  $(5x)^{-\frac{1}{2}}$

15)  $(10n)^{\frac{3}{2}}$

16)  $a^{\frac{6}{5}}$

17)  $(6v)^{1.5}$

18)  $m^{-\frac{1}{2}}$

Write each expression in exponential form.

19)  $(\sqrt[4]{m})^3$

20)  $(\sqrt[3]{6x})^4$

21)  $\sqrt[4]{v}$

22)  $\sqrt{6p}$

23)  $(\sqrt[3]{3a})^4$

24)  $\frac{1}{(\sqrt{3k})^5}$

Simplify.

25)  $9^{\frac{1}{2}}$

26)  $343^{-\frac{4}{3}}$

27)  $1000000^{\frac{1}{6}}$

28)  $36^{\frac{3}{2}}$

29)  $(x^6)^{\frac{1}{2}}$

30)  $(9n^4)^{\frac{1}{2}}$

31)  $(64n^{12})^{-\frac{1}{6}}$

32)  $(81m^6)^{\frac{1}{2}}$

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### Simplifying Radical Expressions

Simplify each Radical Expression. If necessary use absolute value signs.

1)  $\sqrt{64}$

6)  $\sqrt[3]{375c^6p^2}$

2)  $\sqrt[3]{40c^7}$

7)  $\sqrt[3]{189g^7d^4}$

3)  $\sqrt[3]{81}$

8)  $\sqrt{45b}$

4)  $\sqrt[3]{189c^6q^7}$

9)  $\sqrt{49h^2}$

5)  $\sqrt{81q^2}$

10)  $\sqrt{245t^5s}$



## 8.6 Practice - Rational Exponents

Write each expression in radical form.

1)  $m^{\frac{3}{5}}$

2)  $(10r)^{-\frac{3}{4}}$

3)  $(7x)^{\frac{3}{2}}$

4)  $(6b)^{-\frac{4}{3}}$

Write each expression in exponential form.

5)  $\frac{1}{(\sqrt{6x})^3}$

6)  $\sqrt{v}$

7)  $\frac{1}{(\sqrt[4]{n})^7}$

8)  $\sqrt{5a}$

Evaluate.

9)  $8^{\frac{2}{3}}$

10)  $16^{\frac{1}{4}}$

11)  $4^{\frac{3}{2}}$

12)  $100^{-\frac{3}{2}}$

Simplify. Your answer should contain only positive exponents.

13)  $yx^{\frac{1}{3}} \cdot xy^{\frac{3}{2}}$

14)  $4v^{\frac{2}{3}} \cdot v^{-1}$

15)  $(a^{\frac{1}{2}}b^{\frac{1}{2}})^{-1}$

16)  $(x^{\frac{5}{3}}y^{-2})^0$

17)  $\frac{a^2b^0}{3a^4}$

18)  $\frac{2x^{\frac{1}{2}}y^{\frac{1}{3}}}{2x^{\frac{4}{3}}y^{-\frac{7}{4}}}$

19)  $uv \cdot u \cdot (v^{\frac{3}{2}})^3$

21)  $(x^0y^{\frac{1}{3}})^{\frac{3}{2}}x^0$

20)  $(x \cdot xy^2)^0$

23)  $\frac{a^{\frac{3}{4}}b^{-1} \cdot b^{\frac{7}{4}}}{3b^{-1}}$

22)  $u^{-\frac{5}{4}}v^2 \cdot (u^{\frac{3}{2}})^{-\frac{3}{2}}$

25)  $\frac{3y^{-\frac{5}{4}}}{y^{-1} \cdot 2y^{-\frac{1}{3}}}$

24)  $\frac{2x^{-2}y^{\frac{5}{3}}}{x^{-\frac{5}{4}}y^{-\frac{5}{3}} \cdot xy^{\frac{1}{2}}}$

27)  $\left(\frac{m^{\frac{3}{2}}n^{-2}}{(mn^{\frac{4}{3}})^{-1}}\right)^{\frac{7}{4}}$

26)  $\frac{ab^{\frac{1}{3}} \cdot 2b^{-\frac{5}{4}}}{4a^{-\frac{1}{2}}b^{-\frac{2}{3}}}$

29)  $\frac{(m^2n^2)^0}{n^{\frac{3}{4}}}$

28)  $\frac{(y^{-\frac{1}{2}})^{\frac{3}{2}}}{x^{\frac{3}{2}}y^{\frac{1}{2}}}$

31)  $\frac{(x^{-\frac{4}{3}}y^{-\frac{1}{3}} \cdot y)^{-1}}{x^{\frac{1}{3}}y^{-2}}$

30)  $\frac{y^0}{(x^4y^{-1})^{\frac{1}{3}}}$

33)  $\frac{(uv^2)^{\frac{1}{2}}}{v^{-\frac{1}{4}}v^2}$

32)  $\frac{(x^{\frac{1}{2}}y^0)^{-\frac{4}{3}}}{y^4 \cdot x^{-2}y^{-\frac{2}{3}}}$

## Simplifying Rational Exponents

Simplify.

1)  $(n^4)^{\frac{3}{2}}$

2)  $(27p^6)^{\frac{5}{3}}$

3)  $(25b^6)^{-1.5}$

4)  $(64m^4)^{\frac{3}{2}}$

5)  $(a^8)^{\frac{3}{2}}$

6)  $(9r^4)^{0.5}$

7)  $(81x^{12})^{1.25}$

8)  $(216r^9)^{\frac{1}{3}}$

Simplify. Your answer should contain only positive exponents with no fractional exponents in the denominator.

9)  $2m^2 \cdot 4m^{\frac{3}{2}} \cdot 4m^{-2}$

10)  $3b^{\frac{1}{2}} \cdot b^{\frac{4}{3}}$

11)  $\left(\frac{3}{p^2}\right)^{-2}$

12)  $\left(a^{\frac{1}{2}}\right)^{\frac{3}{2}}$

$$13) \frac{2x^{-\frac{7}{4}}}{4x^{\frac{4}{3}}}$$

$$14) \frac{4x^2}{2x^{\frac{1}{2}}}$$

$$15) \frac{3x^{-\frac{1}{2}} \cdot 3x^{\frac{1}{2}} y^{-\frac{1}{3}}}{3y^{-\frac{7}{4}}}$$

$$16) \frac{3y^{\frac{1}{4}}}{4x^{-\frac{2}{3}} y^{\frac{3}{2}} \cdot 3y^{\frac{1}{2}}}$$

$$17) \left(m \cdot m^{-2} n^{\frac{5}{3}}\right)^2$$

$$18) \left(a^{-1} b^{\frac{1}{3}} \cdot a^{-\frac{4}{3}} b^2\right)^2$$

$$19) \left(\frac{x^{\frac{1}{2}} y^{-2}}{yx^{-\frac{7}{4}}}\right)^4$$

$$20) \frac{(x^3 y^2)^{\frac{3}{2}}}{\left(x^{-1} y^{-\frac{2}{3}}\right)^{\frac{1}{4}}}$$

$$21) \frac{\left(x^{-\frac{1}{2}} y^2\right)^{-\frac{5}{4}}}{x^2 y^{\frac{1}{2}}}$$

$$22) \frac{\left(x^{-\frac{1}{2}} y^4\right)^{\frac{1}{4}}}{x^{\frac{2}{3}} y^{\frac{3}{2}} \cdot x^{-\frac{3}{2}} y^{\frac{1}{2}}}$$



## Practice with Rational Exponents

1) Rewrite each radical using rational exponent notation.

a.  $\sqrt[3]{7} =$

b.  $(\sqrt{11})^5 =$

c.  $\sqrt[4]{x^8} =$

2) Rewrite each power using radical notation.

a.  $43^{1/5} =$

b.  $8^{-3/4} =$

c.  $x^{5/2} =$

3) Find the exact, simplified value of each expression **without a calculator**. *If you are stuck, try converting between radical and rational exponential notation first, and then simplify.*  
Sometimes, simplifying the exponent (or changing a decimal to a fraction) is very helpful.

a.  $8^{2/3} =$

b.  $(-27)^{2/3} =$

c.  $25^{-3/2} =$

d.  $\left(\frac{8}{27}\right)^{-2/3} =$

e.  $4^{1.5} =$

f.  $\left(\frac{1}{4}\right)^{-1.5} =$

g.  $(\sqrt[3]{64})^4 =$

h.  $(\sqrt{3})^6 =$

i.  $(\sqrt[4]{3})^8 =$

4) Simplify each expression completely.

a.  $5^{1/4} \times 5^{7/4} =$

b.  $(2^{1/3})^{3/4} =$

c.  $\frac{7^{1/5}}{7^{3/5}} =$

d.  $(2^{1/4} \times 2^{1/3})^6 =$

e.  $\frac{12^{11/8}}{12^{-5/8}} =$

f.  $\frac{5x^{3/4}yz^{-1/3}}{10x^{1/4}z^{2/3}} =$

## Homework #9-1: Rational Exponents

### Part 1

- 1) Find the exact, simplified value of each expression **without a calculator**. *If you are stuck, try converting between radical and rational exponential notation first, and then simplify.*  
Sometimes, simplifying the exponent (or changing a decimal to a fraction) is very helpful.

a.  $125^{\frac{1}{3}} =$

b.  $64^{-1/2} =$

c.  $64^{1/6} =$

d.  $81^{1/2} =$

e.  $32^{-1/5} =$

f.  $81^{-1/4} =$

g.  $4^{3/2} =$

h.  $(-64)^{2/3} =$

i.  $(-8)^{-5/3} =$

j.  $9^{-3/2} =$

k.  $\left(\frac{9}{4}\right)^{3/2} =$

l.  $16^{-1.5} =$

m.  $(\sqrt[3]{-27})^2 =$

n.  $\sqrt[3]{125^2} =$

o.  $(\sqrt[3]{4})^6 =$

p.  $(\sqrt{5})^{-2} =$

q.  $(\sqrt[4]{2})^{-4} =$

r.  $(\sqrt[5]{3})^5 =$

- 2) Simplify each expression completely.

a.  $3^{5/3} \times 3^{1/3} =$

b.  $(5^{2/3})^{1/2} =$

c.  $\frac{1}{36^{-1/2}} =$

d.  $\left(\frac{5^2}{8^2}\right)^{-1/2} =$

e.  $\frac{125^{1/9}}{5^{1/4}} =$

f.  $(10^{3/4} \times 4^{3/4})^4 =$